# Dominance Testing for "Pro-Poor" Growth with an Application to European Growth

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## Abstract

This paper introduces statistical testing procedures to evaluate 'pro-poor' growth. Our measure of "pro-poorness" follows Kakwani (2000), Kakwani and Pernia (2000), and Son (2004), who decompose the generalized Lorenz ordinates into a growth effect and an inequality effect. We derive an asymptotic distribution-free covariance matrix for the decomposed generalized Lorenz curves. Using this decomposition (and our standard errors) we test for *pro-poor dominance* in the growth process. We illustrate our test for pro-poor dominance by evaluating the degree of pro-poor growth in five European countries.

**Key Words:** Pro-poor Growth, Poverty, Stochastic dominance. **JEL Classification:** D31, D63, I32

### 1. INTRODUCTION

"My dream has always been to make the poor richer, not to make the rich poorer...A rising tide lifts all boats."

John F. Kennedy

President Kennedy's statement was re-posed as a question by Danziger and Gottschalk in their 1986 American Economic Association conference paper as: "Do rising tides lift all boats?" From the beginning of the US War on Poverty economists have noted that increased growth does not necessarily result in a decline in poverty (see Anderson, 1964 and Ahluwalia, 1974). More recently, this question has been recast to ask which types of economic policies lead to 'pro-poor' growth especially in light of the well-publicized Millennium Development Goals (MDG's). The past decade has produced a great deal of research relating to how to measure "pro-poorness." Essama-Nssah and Lambert (2009) and Duclos (2009) provide thorough reviews of this literature.

The purpose of this paper is introduce statistical testing procedures to evaluate 'pro-poor' growth. Our statistical approach is based on the seminal work of Beach and Davidson (1983) who provide asymptotic distribution-free covariance matrices for Lorenz and generalized Lorenz curves. Our theoretical approach to measuring "pro-poorness" follows Kakwani (2000), Kakwani and Pernia (2000) and Son (2004). The "KPS approach" decomposes changes in the difference in generalized Lorenz ordinates into a growth effect and an inequality effect. Using this decomposition we can test for *pro-poor dominance* in the growth process. Furthermore, we implement the KPS approach directly using the tools of stochastic dominance, as opposed to the more restrictive index number approach often used in this analysis.

We illustrate our test for pro-poor dominance by evaluating the degree of propoor growth in five European countries.<sup>1</sup> We consider two time periods, 1993 to 2000 and 2000 to 2006. For the combined 1993-2006 period we find that Spain, France, and Italy enjoyed pro-poor growth, Germany's growth experience was anti-poor, and the UK pro-poor ranking is ambiguous.

<sup>&</sup>lt;sup>1</sup> Only one researcher to our knowledge has studied pro-poor growth in Europe (Heinrich, 2003). No researcher has employed dominance methods together with formal inference tests.

## 2. THEORETICAL FRAMEWORK

### 2.1 Second-order dominance (Generalised Lorenz dominance)

As Kakwani's method of evaluating pro-poor growth has its roots in second order stochastic dominance, we briefly introduce this technique. Following Atkinson (1970) we assume that the relationship between the distribution of income and the standard of living is given by a social welfare function, which represents the ethical judgments regarding income distributions. The well-known Atkinson Lorenz Dominance Theorem as extended by Dasgupta, Sen and Starrett (1973) is restricted to comparing distributions with the same mean. However, as Sen (1973) points out, the means of two distributions will rarely be equal. Shorrocks (1983) addresses this problem by introducing generalised Lorenz Dominance.

From Gastwirth (1971), the Lorenz curve can be defined as:

$$L_{X}(p) := \mu^{-1} \int_{0}^{p} X(u) du, \qquad [1]$$

and the generalised Lorenz curve will then be (Shorrocks, 1983):

$$GL_{X}(p) := \int_{0}^{p} X(u) du = \mu_{X} L_{X}(p), \quad \forall p \in [0,1]$$
[2]

Let  $W_s$  be a S-concave and increasing welfare function. Then we have the next theorem, demonstrated by Shorrocks (1983):

**Theorem 1—GL Dominance**:  $w(X) \ge w(Y), \forall w \in W_s$  iff  $GL_X(p) \ge GL_Y(p)$  for all p with at least one inequality prevailing.

The implications of this approach are straightforward: assuming two widely, though not universally, accepted value judgments (the Pareto principle and the Pigou-Dalton transferences principle) we can rank the economic welfare associated to two different income distributions.

## 2.2 Truncated second-order dominance and poverty

Foster and Shorrocks (1988) links second order dominance to poverty. As it is well known, income-gap is the weighted sum of the income shortfalls of the poor, that is:

$$P(x;z) = \left[\frac{1}{n(x)}\right] \sum_{i=1}^{r} \frac{z - x_i}{z}$$
[3]

Being *r* the order statistic corresponding to the poverty line, *z*, and *x<sub>i</sub>* the *i*-th individual's income. This criterion implies that income distribution *X* dominates income distribution *Y*, denoted by  $X >_{z^*} Y$ , if, and only if,  $(1/n)\sum x_i > (1/n)\sum y_i$  for all *i* up to *r* and for any given  $z^*$ . Then:

$$GL_X(p) \ge GL_Y(p)$$
 iff  $X \ge _{z^*} Y, \forall z < z^*$ 

This implies that if the distribution is truncated at any arbitrary poverty line  $z < z^*$  and X generalised Lorenz dominates Y at and below that poverty line, then the income-gap poverty in X cannot exceed poverty in Y using that poverty line, and this is the case for every poverty line  $z < z^*$ .

## 2.3 Inequality effect and growth effect: an stochastic dominance approach

Our approach to measure "pro-poorness" follows Kakwani (2000), Kakwani and Pernia (2000) and Son (2004). The KPS approach decomposes changes in the difference in generalized Lorenz ordinates into a growth effect and an inequality effect. One key point in understanding the evaluation of "pro-poorness" is to clearly identify the reference point. The proposed method uses the underlying income distribution as reference point.<sup>2</sup>

<sup>&</sup>lt;sup>2</sup> Bishop and Formby (1994) evaluate the "benefits of growth" using generalized concentration curves and like the Kakwani method use the Lorenz curve as the reference point. See Duclos (2009) and Essama-Nssah and Lambert (2009) for approaches to measuring pro-poorness with alternative reference points.

To evaluate changes in welfare due to economic growth we begin with the generalized Lorenz curve:  $GL = \mu L(p)$ . Between two periods, its variation will be given as:

$$\Delta GL(p) = GL_2(p) - GL_1(p) = \mu_2 L_2(p) - \mu_1 L_1(p)$$
[6]

that is, the total change is due to both the change in the average income and the change in the income distribution measured by the Lorenz curve. So the total effect can be decomposed in *growth effect* and *inequality effect*. Following Kakwani's (2000) axiomatic approach, this decomposition can be done as follows:

$$\Delta GL_{I} = \frac{1}{2} \{ \mu_{1}L_{2}(p) - \mu_{1}L_{1}(p) + \mu_{2}L_{2}(p) - \mu_{2}L_{1}(p) \}$$
[7]

$$\Delta GL_g = \frac{1}{2} \{ \mu_2 L_1(p) - \mu_1 L_1(p) + \mu_2 L_2(p) - \mu_1 L_2(p) \}$$
[8]

and the sum of [7] and [8] equals the total change:

$$\Delta GL_I + \Delta GL_g = \Delta GL(p)$$
[9]

The *inequality effect*,  $GL_I$ , shows the variation of inequality, measured by the Lorenz curve, using the income in both the beginning and the final period. The interpretation of the growth effect  $GL_g$  is analogous.

As it is well known, the generalized Lorenz curve is defined by the pair of coordinates  $\{p; \mu L(p)\}$ . Then, the generalized Lorenz curve ordinates taking into account only the *inequality effect* will be:

$$GL_{I}(p) = GL_{1}(p) + \frac{1}{2} \{ \mu_{1}L_{2}(p) - \mu_{1}L_{1}(p) + \mu_{2}L_{2}(p) - \mu_{2}L_{1}(p) \}$$
[10]

On the other hand, it is straightforward that:

$$GL_{I}(p) + \Delta GL_{g} = GL_{I}(p) + \frac{1}{2} \{ \mu_{1}L_{2}(p) - \mu_{1}L_{1}(p) + \mu_{2}L_{2}(p) - \mu_{2}L_{1}(p) \} + \frac{1}{2} \{ \mu_{2}L_{1}(p) - \mu_{1}L_{1}(p) + \mu_{2}L_{2}(p) - \mu_{1}L_{2}(p) \} = GL_{1}(p) + GL_{2}(p) - GL_{1}(p) = GL_{2}(p), \qquad [11]$$

$$\forall p$$

Some interesting insights arise from the expressions above. If the inequality effect generalized Lorenz curve given by [10] dominates the ordinary generalized Lorenz curve  $GL_1$ , the inequality effect then reduces poverty as measured by Atkinson (1987). We call this result *pro-poor dominance*. The welfare implications are straightforward: pro-poor dominance implies an increase in economic welfare as measured the welfare functions included in  $W_s$ .

The next theorem demonstrates this result:

**Theorem 2—Pro-Poor Dominance:** If  $GL_1(p) \ge GL_1(p)$ ,  $\forall x < z^*$ , with at least one inequality holding, then:  $X_1 \ge_{z^*} X_1$  and  $X_1 W_2^* X_1$ , where y is the initial income distribution and x the distribution taking into account only the *inequality effect*.

This theorem implies that if the generalized Lorenz curve taking into account only the *inequality effect* dominates the first period generalized Lorenz curve, the growth will have been pro-poor, not only because the decrease of poverty, but also because the increase of economic welfare of the poor, given the assumptions made above.<sup>3</sup>

The relationship between stochastic dominance and welfare can be extended to the truncated distributions. If the inequality effect generalized Lorenz curve  $GL_1(p)$  dominates the ordinary GL curve,  $GL_1(p)$ , for all incomes up to  $z^*$  (defining  $z^*$  as the poverty line), then growth is poverty-reducing for all the poverty indexes as defined in Atkinson (1987).

<sup>&</sup>lt;sup>3</sup> Note that our result is equivalent to Son's (2004) poverty growth curve. As noted by Son the generalized Lorenz approach is based on second order stochastic dominance while Ravallion and Chen's (2003) growth incidence curve. Son also points the advantages and disadvantages of the two approaches. Son recommends but does not provide formal inference tests.

#### 2.4 Inference tests for Pro-Poor Dominance

When comparing generalized Lorenz curves there are three possible, outcomes, equivalence, dominance, or crossing. Bishop, Formby and Thistle (1989) recommend a pair wise statistical inference test procedure to evaluate generalised Lorenz curves, given these three alternatives. We adapt this approach to test for pro-poor dominance. Using a set of k sub-hypotheses to test for the overall hypothesis of equivalence we have:

$$H_{0,i}: GL_1 = GL_1 \text{ and } H_{A,i}: GL_1 \neq GL_1$$
[12]

If each of the sub-hypotheses is not rejected then the joint null hypotheses is not rejected, and we conclude that the growth process is neither pro or anti poor. On the other hand, if the any of the sub-hypotheses are rejected, then the following are the possible outcomes:

- Weak Pro-Poor dominance: If for some quantiles  $GL_I > GL_1$  and for others  $GL_I = GL_1$ , then we conclude that growth is weakly pro-poor. If  $GL_I > GL_1$  for all *I* then we have strong pro-poor growth.
- If for some quantiles  $GL_I > GL_1$  and for others  $GL_I < GL_1$ , then no unambiguous ranking is possible for all z (it will be neccesary to analyze truncated dominance).

The statistical tests will be:

$$T_{GLi} = \frac{\hat{G}L_I - \hat{G}L_1}{\left[\left(\frac{\underline{\sigma}_{ii}^{I}}{N_I}\right) + \left(\frac{\underline{\sigma}_{ii}^{1}}{N_1}\right)\right]^{1/2}} \text{ where } i=1,2,\dots,K.^4$$
[13]

Beach and Davidson (1983) derive the statistical distribution for  $\hat{G}L_1$ . However, the distribution for  $\hat{G}L_1$  is unknown needs to be derived. Equation [10] implies:

$$GL_{I}(p) = GL_{1}(p) + \frac{1}{2} \{ \mu_{1}L_{2}(p) - \mu_{1}L_{1}(p) + \mu_{2}L_{2}(p) - \mu_{2}L_{1}(p) \}$$
[10]'

<sup>&</sup>lt;sup>4</sup> The critical values for this test are determined by the Student Maximum Modulus distribution. Tables can be obtained from Stoline and Ury (1979).

and can be written as:

$$GL_{I}(p) = GL_{1}(p) + \frac{1}{2} \left\{ GL_{1,2}(p) - GL_{1}(p) + GL_{2}(p) - GL_{2,1}(p) \right\} = \frac{1}{2} \left\{ GL_{1,2}(p) + GL_{1}(p) + GL_{2}(p) - GL_{2,1}(p) \right\}$$
[14]

where:

$$GL_{1,2}(p) = \mu_1 L_2(p)$$
 [15]

That is,  $GL_{1,2}(p)$  is the generalized Lorenz curve obtained by scaling the income distribution of the second period by the mean income of the first. In an analogous way, we have:

$$GL_{2,1}(p) = \mu_2 L_1(p)$$
[16]

Taking this into account, the variance of  $GL_{I}(p)$  can be written as:

$$Var(GL_{I}) = \frac{1}{4} \begin{cases} Var(GL_{1,2}(p)) + Var(GL_{1}(p)) + Var(GL_{2}(p)) + Var(GL_{2,1}(p)) + \\ 2Cov[GL_{1,2}(p);GL_{1}(p)] + 2Cov[GL_{1,2}(p);GL_{2}(p)] - \\ 2Cov[GL_{1,2}(p);GL_{2,1}(p)] + 2Cov[GL_{1}(p);GL_{2}(p)] - \\ 2Cov[GL_{1}(p);GL_{2,1}(p)] - 2Cov[GL_{2}(p);GL_{2,1}(p)] \end{cases}$$
[17]

Some items in [17] are equal to zero, since the initial and final distributions are independent:

$$Cov[GL_1(p);GL_2(p)] = 0$$
 [18]

 $Cov[GL_{1,2}(p);GL_1(p)] = Cov[\mu_1L_2(p);\mu_1L_1(p)] = 0$ , since it is the covariance of the initial and final distribution scaled by the same quantity. Moreover:

$$Cov[GL_{1,2}(p);GL_{2,1}(p)] = Cov[\mu_1 L_2(p);\mu_2 L_1(p)] = 0$$
[19]

$$Cov[GL_{2}(p);GL_{2,1}(p)] = Cov[\mu_{2}L_{2}(p);\mu_{2}L_{1}(p)] = 0$$
[20]

There are still two items to be calculated. The first one is:

$$Cov[GL_{1,2}(p);GL_2(p)] = Cov[\mu_1 L_2(p);\mu_2 L_2(p)]$$
[21]

From a very well known property of the variance:

$$Var[\mu_{1}L_{2}(p) + \mu_{2}L_{2}(p)] = Var[(\mu_{1} + \mu_{2})L_{2}(p)] =$$
  
=  $Var(\mu_{1}L_{2}(p)) + Var(\mu_{2}L_{2}(p)) + 2Cov[\mu_{1}L_{2}(p);\mu_{2}L_{2}(p)]$  [22]

from where:

$$2Cov[\mu_1 L_2(p); \mu_2 L_2(p)] = Var(\mu_1 L_2(p)) + Var(\mu_2 L_2(p)) - Var[(\mu_1 + \mu_2)L_2(p)]$$
[23]

Analogously, we have:

$$2Cov[\mu_1 L_1(p); \mu_2 L_1(p)] = Var(\mu_1 L_1(p)) + Var(\mu_2 L_1(p)) - Var[(\mu_1 + \mu_2)L_1(p)]$$
[24]

Using all these results in [17]:

$$Var(GL_{1}) = \frac{1}{4} \begin{cases} Var(GL_{1,2}(p)) + Var(GL_{1}(p)) + Var(GL_{2}(p)) + Var(GL_{2,1}(p)) + \\ + 2Cov[GL_{1,2}(p);GL_{2}(p)] - 2Cov[GL_{2}(p);GL_{2,1}(p)] \end{cases}$$
[25]

And after some manipulations, the next expression is reached:

$$Var(GL_{1}) = \frac{1}{4} \{ 2Var(\mu_{2}L_{2}(p)) + 2Var(\mu_{1}L_{2}(p)) - Var[(\mu_{1} + \mu_{2})L_{2}(p)] + Var[(\mu_{1} + \mu_{2})L_{1}(p)] \}$$
[26]

As it can be seen in [26], the variance of the generalized Lorenz curve that only has into account the *inequality effect* is computed using the variances of four different income distributions.

Now, it is possible to calculate both the variance of  $GL_1$  and  $GL_1$ . The variance of  $GL_1$  is given by Beach and Davidson (1983). For  $GL_1$ , it will be given, for i=j, by the expression<sup>5</sup>:

$$Var(GL_{I}) = \varpi_{ii}^{I} = \frac{1}{4} \left\{ 2\varpi_{ij}^{2,2} + 2\varpi_{ij}^{1,2} - \varpi_{ij}^{1,2^{*}} + \varpi_{ij}^{1^{*},2} \right\}$$
[27]

being  $\overline{a}_{ij}^{a,a}$  the variance of the generalized Lorenz curve of the distributions seen in [26].

## 3. RECENT TRENDS IN EUROPEAN POVERTY AND INEQUALITY

According to the OECD (2008) economic inequality in Europe is on the rise. For our sample of countries the Gini coefficients in mid-2000s vary between 0.28 for France and 0.35 for Italy. Germany shows a Gini coefficient of 0.3, Spain of 0.32 and Great Britain of 0.34. While the differences are not wide at all, it is interesting to note that there has been changes in the inequality trends among these countries in the last two decades.

Two periods can be distinguished in the evolution of income distribution, mid-1980's to mid 1990's and the mid-1990's to mid 2000's. In the first period inequality fell in Spain and France, while it increased in Germany, Italy and UK. In the second period, inequality remained steady in Spain and France, increased in Germany and in Italy, and decreased in the UK. From the mid 1990's to mid 2000's Germany's inequality continues to increase, France and Spain enjoy a decrease in inequality, while there was no significant change in inequality in Italy and the UK.<sup>6</sup>

If we turn our attention to headcount poverty evolution in the last decade (with 50% of median income as poverty line) France, Italy and the UK experienced decreases in poverty while poverty in Germany and Spain increased. The analysis of relative poverty is interesting, but also it is to know what has happened in absolute terms. One

<sup>&</sup>lt;sup>5</sup> The final expression of the variances are developed in the appendix.

<sup>&</sup>lt;sup>6</sup> These conclusions are based on the Eurostat database.

way to do this is to fix a relative poverty line for a period *t* and, adjusted for inflation, to use it to compare poverty in, say, period  $t+n^7$ . Following this approach, *absolute* poverty decreased in all countries analyzed between mid 1990's and mid 2000's with the exception of Germany, where absolute poverty increased.

## 4. DATA AND EMPIRICAL ANALYSIS

#### 4.1 Data

To identify the 'pro-poor' aspects of economic growth we need data of a sufficient time span to capture the effects of distributional changes imbedded in the growth process. To this aim we have used data from two different, although consistent, datasets: The European Community Household Panel (ECHP) and the Survey on Income and Living Conditions (SILC), both developed by Eurostat. We have drawn data for the years 1993 and 2000 from the ECHP (waves first and eight of the survey) while for 2006 we use data from the SILC (the 2007 wave).

Our income measure is *per capita* household disposable income including total market income, adding transfers, and deducting taxes and Social Security contributions, adjusted by the modified OECD equivalence scale. The data are weighted using the weights given by the sample design and the number of individuals in the households, so we convert household data into individual data, assuming the same income for each member of the household. Finally, data have been deflated to 1993 units using the HIPC from Eurostat.

#### 4.2 Results

In this section we apply formal inference tests to address two questions. First, did welfare improve (i.e., generalized Lorenz dominance) in each of the five European counties selected between 1993 and 2006? Secondly, and of more direct interest to us, was economic growth during this period 'pro-poor'? In this second case we compare the ordinary generalized Lorenz curve of the initial period to the inequality effect generalized Lorenz curve of the second period.

<sup>&</sup>lt;sup>7</sup> This approach is comparable to the empirical analysis carried out in this paper.

Table 1 shows the results of the GL dominance tests and the pro-poor tests for Germany, 1993-2000. Columns 2 and 3 provide the 1993 and 2000 generalized Lorenz ordinates while the fourth column provide the test statistics for ordinary GL dominance. As each of the test statistics is greater than the five percent SMM critical value of 2.80 we conclude 2000 generalized Lorenz dominates 1993, implying improving welfare over time.

To test for pro-poor dominance we compare the GL ordinate for 1993 (column 2) with the  $G_I$  ordinate (column 5). All of the nine test statistics are positive, and eight of the nine test statistics are statistically significant at the five percent level. From these results we conclude that growth in Germany between 1993 and 2000 was unambiguously 'pro-poor'.

Table 2 examines German growth over the period 2000-2006 and provides results that are quite different from the period 1993-2000. First, we note that the ordinary GL curves cross—Germany in 2006 has a higher mean income (GL<sub>10</sub>) but the other nine GL ordinates are smaller in 2006 as compared to 2000. Figure 1 illustrates this GL crossing (GL<sub>00</sub> vs. GL<sub>06</sub>) and highlights the fact that crossing GL curves prevent an unambiguous welfare ranking.

While no unambiguous welfare conclusion can be drawn from the German growth experience of 2000 to 2006, we are able to rank this time period as unfavourable to the poor. All of the nine test statistics in column 6 are negative and significant indicating that economic growth over this period is clearly anti-poor. These results are illustrated Figure 2 with  $GL_I$  lying below  $GL_{00}$ , indicating that the German poor lost ground over this time period.

Table 3 provides the test results for GL and pro-poor dominance over the entire time period, 1993 to 2006. The generalized Lorenz curve of 2006 weak dominates to the one of 1993—weak dominance implies some positive and significant differences and no negative and significant differences (see column 4). However, the failure of the lowest German incomes to grow--GL deciles 1 and 2 show no change in income for the poorest persons—suggests that the poor did not fare well over this time period. The failure of the poor to share the benefits of growth is verified by testing for pro-poor dominance. Column 6 reports the results of this test and shows the time period is ranked as "antipoor."<sup>8</sup>

<sup>&</sup>lt;sup>8</sup> In the case of Germany 1993 to 2006 if we define the poverty line the 20<sup>th</sup> percentile (truncated dominance) we can conclude that the time period 1993 to 2006 was neither pro-poor or anti-poor (no significant difference.

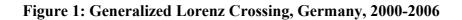
Table 4 provides a summary of the numerical and statistical comparisons for all five Europe countries examined (see the Appendix for detailed tables for France, Italy, Spain and the UK). To understand how the table works consider the last comparisons made, Germany, 1993 to 2006, which is shown in the last columns of the first row. Under GL dominance we report '+ +' which means that both the numerical and statistical comparisons ranked 2006 over 1993. However, under pro-poor dominance we report 'x -' which implies that the numerical crossing was replaced by an statistical ranking of anti-poor. This table demonstrates the errors in rankings that can occur in the absence of statistical tests like those developed in the this paper. In fact, six out of 30 or 20 percent of the comparisons in Table 4 are mis-ranked using numerical comparisons.

While Table 4 highlights the necessity of formal inference tests, it also summarizes the growth experience of the five European countries. All five countries show both GL dominance and pro-poor dominance for the 1993 to 2000 period. For the period 2000-2006 all countries but Germany experienced GL dominance; however, economic growth was anti-poor in Italy and the UK as well as in Germany. For the combined 1993-2006 period all countries show GL dominance, Spain, France and Italy are pro-poor, Germany is anti-poor, and the UK pro-poor ranking is ambiguous.

## 5. CONCLUSIONS

This paper introduces statistical testing procedures to evaluate 'pro-poor' growth. Our theoretical approach to measuring "pro-poorness" follows Kakwani (2000), Kakwani and Pernia (2000), and Son (2004). The "KPS approach" decomposes changes in the difference in generalized Lorenz ordinates into a growth effect and an inequality effect. Using this decomposition we can test for *pro-poor dominance* in the growth process. Furthermore, we test for pro-poor dominance directly using the tools of stochastic dominance, as opposed to the more restrictive index number approach often used in this analysis. We derive an asymptotic distribution-free covariance matrix for the decomposed generalized Lorenz curves on which pro-poor dominance testing is based.

We illustrate our test for pro-poor dominance by evaluating the degree of propoor growth in five European countries. We consider two time periods, 1993 to 2000 and 2000 to 2006. For the combined 1993-2006 period we find that Spain, France, and Italy enjoyed pro-poor growth, Germany's growth experience was anti-poor, and the UK pro-poor ranking is ambiguous.



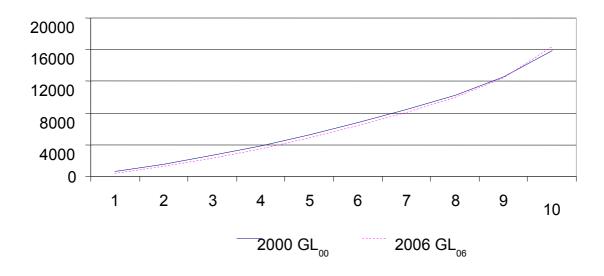
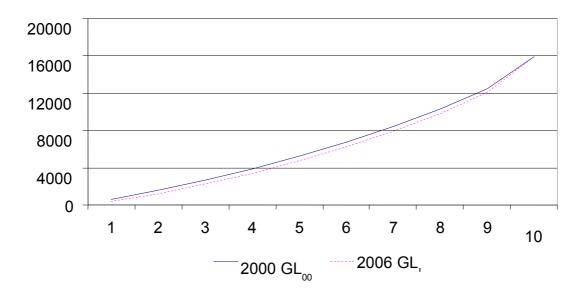


Figure 2: Pro-Poor Dominance, Germany 2000-2006



Genera	Germany, Generalized Lorenz Dominance			1993-2000 Pro-Poor Dominance				
Decile	ĜL93	ĜL <sub>00</sub>	T <sub>GL1</sub>	ĜL <sub>1</sub>	T <sub>GL1</sub>			
(1)	(2)	(3)	(4)	(5)	(6)			
1	384.63	632.26	22.06*	614.39	15.54*			
2	1209.68	1560.87	19.68*	1511.78	14.26*			
3	2220.50	2660.08	18.88*	2575.71	13.44*			
4	3375.42	3909.28	18.47*	3779.20	12.70*			
5	4668.51	5274.97	18.06*	5094.59	11.80*			
6	6119.51	6757.93	16.00*	6526.13	9.68*			
7	7775.97	8418.21	13.40*	8125.50	7.04*			
8	9661.71	10298.79	11.34*	9937.77	4.81*			
9	11918.11	12515.64	8.74*	12076.24	2.29*			
10	15384.11	15950.20	5.25*	15384.11	0.00			

Table 1Generalized Lorenz and Pro-Poor Dominance,Germany, 1993-2000

Five percent critical value for SMM=2.80

		Germany,	2000-2006				
Genera	lized Lorenz l	Dominance	<b>Pro-Poor Dominance</b>				
Decile (1)	ĜL <sub>00</sub> (2)	ĜL <sub>06</sub> (3)	T <sub>GL1</sub> (4)	<b>ĜL</b> <sub>1</sub> (5)	T <sub>GL1</sub> (6)		
1	632.26	414.11	-15.44*	400.17	-19.44*		
2	1560.87	1257.81	-16.58*	1220.63	-19.73*		
3	2660.08	2298.13	-16.02*	2230.68	-19.03*		
4	3909.28	3496.15	-15.24*	3399.74	-18.22*		
5	5274.97	4849.66	-13.64*	4719.85	-17.32*		
6	6757.93	6370.29	-10.72*	6200.31	-14.84*		
7	8418.21	8084.48	-7.77*	7873.24	-11.98*		
8	10298.79	10055.50	-4.85*	9794.47	-9.47*		
9	12515.64	12410.92	-1.73	12088.61	-6.57*		
10	15950.20	16364.51	3.91*	15950.20	0.00		

 Table 2

 Generalized Lorenz and Pro-Poor Dominance,

 Germany

 2000-2006

Five percent critical value for SMM=2.80

Table 3Generalized Lorenz and Pro-Poor Dominance,<br/>Germany, 1993-2006

Genera	Generalized Lorenz Dominance			Pro-Poor Dominance				
Decile (1)	ĜL <sub>93</sub> (2)	ĜL <sub>06</sub> (3)	T <sub>GL1</sub> (4)	<b>ĜL</b> <sub>1</sub> (5)	T <sub>GL1</sub> (6)			
1	384.63	414.11	1.92	-389.41	0.33			
2	1209.68	1257.81	2.38*	-1181.50	-1.35			
3	2220.50	2298.13	3.20*	-2158.52	-2.43*			
4	3375.42	3496.15	4.20*	-3283.92	-2.98*			
5	4668.51	4849.66	5.47*	-4554.82	-3.21*			
6	6119.51	6370.29	6.48*	-5983.65	-3.24*			
7	7775.97	8084.48	6.80*	-7594.70	-3.66*			
8	9661.71	10055.50	7.49*	-9445.93	-3.76*			
9	11918.11	12410.92	7.84*	-11658.78	-3.78*			
10	15384.11	16364.51	9.97*	-15384.11	0.00			

Five percent critical value for SMM=2.80

	<u>1993</u>	-2000	<u>2000</u> -	-2006	<u>1993</u>	-2006
Country	GL Dominance	Pro-Poor Dominance	GL Dominance	Pro-Poor Dominance	GL Dominance	Pro-Poor Dominance
Germany	++	++	XX	<u> </u>		X –
France	++	++	X +	X +	++	++
Italy	++	++	++		++	X +
Spain	++	++	++	X +	++	++
UK	++	X +	++		++	XX

 Table 4

 Summary of Generalized Lorenz and Pro-Poor Dominance<sup>1</sup>

<sup>1</sup>First entry is numerical comparison, second entry is statistical comparison. "+" denotes dominance of 2<sup>nd</sup> year over first, " – " first year over second, and "X" denotes a crossing.

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## APPENDIX

The variance of the ordinates of the generalized Lorenz curve taking into account only the *inequality effect* is as follows:

$$Var(GL_{I}) = \varpi_{ii}^{I} = \frac{1}{4} \left\{ 2\varpi_{ij}^{2,2} + 2\varpi_{ij}^{1,2} - \varpi_{ij}^{1,2^{*}} + \varpi_{ij}^{1^{*},2} \right\} =$$

$$= \frac{1}{4} \left\{ 2Var(\mu_{2}L_{2}(p)) + 2Var(\mu_{1}L_{2}(p)) - Var[(\mu_{1} + \mu_{2})L_{2}(p)] + Var[(\mu_{1} + \mu_{2})L_{1}(p)] \right\}$$
[A1]

To be able to compute this expression we need to calculate each of its parts. To do this we can begin with  $Var(\mu_1 L_2(p))$ . This is the variance of the generalized Lorenz curve multiplying the Lorenz curve of the second period by the average income of period one.

On the other hand, the variance of the generalized Lorenz curve of the second period is (Beach and Davidson, 1983):

$$\varpi_{ij} = p_i \left[ \lambda_i^2 + (1 - p_j) (\xi_{pi} - \gamma_i)^2 \right]$$
[A2]

where, since i=j,  $p_i = p_j$  is the quintile considered (0.1, 0.2,...);  $\lambda_i^2$  is the conditioned variance of each quintile, and  $\xi_{pi}, \gamma_i$  are the maximum and the conditioned average of each quintile.

To calculate the generalized Lorenz curve  $GL_{1,2}$ , we scale the Lorenz curve of the second period by the income mean of the first period, or begin from the generalized Lorenz curve of the second period and multiply by  $\mu_1$  and divide by  $\mu_2$ . Since this is only a change in scale, this will not affect the inequality as measured by the Lorenz curve, since this is a relative inequality measure. Then, if [A2] represents the variance of the generalized Lorenz curve of the second period, the variance of  $Var(\mu_1L_2(p))$  will be:

$$\varpi_{ij}^{1,2} = p_i \left[ \left( \frac{\mu_1}{\mu_2} \right)^2 \lambda_{i,2}^2 + \left( 1 - p_j \right) \left( \frac{\mu_1}{\mu_2} \xi_{pi,2} - \frac{\mu_1}{\mu_2} \gamma_{i,2} \right)^2 \right]$$
[A3]

It is important to note that we are changing the scale of the distribution of the second period, so it will be the sample of this second period that is relevant to compute the statistical test.

Reasoning in a similar way, we have:

$$\overline{\omega}_{ij}^{1,2^*} = p_i \left[ \left( \frac{\mu_1 + \mu_2}{\mu_2} \right)^2 \lambda_{i,2}^2 + \left( 1 - p_j \right) \left( \frac{\mu_1 + \mu_2}{\mu_2} \xi_{pi,2} - \frac{\mu_1 + \mu_2}{\mu_2} \gamma_{i,2} \right)^2 \right]$$
[A4]

$$\overline{\omega}_{ij}^{1^{*},2} = p_{i} \left[ \left( \frac{\mu_{1} + \mu_{2}}{\mu_{1}} \right)^{2} \lambda_{i,1}^{2} + \left( 1 - p_{j} \right) \left( \frac{\mu_{1} + \mu_{2}}{\mu_{1}} \xi_{pi,1} - \frac{\mu_{1} + \mu_{2}}{\mu_{1}} \gamma_{i,1} \right)^{2} \right]$$
[A5]

Then the variance of each ordinate of the generalized Lorenz curve that takes into account only the *inequality effect* will be:

$$Var(GL_{I}) = \varpi \prod_{ii}^{I} = \frac{1}{4} \begin{cases} 2\left(p_{i}\left[\lambda_{i,2}^{2} + (1-p_{j})\left(\xi_{pi,2} - \gamma_{i,2}\right)^{2}\right]\right) + \\ 2\left(p_{i}\left[\left(\frac{\mu_{1}}{\mu_{2}}\right)^{2}\lambda_{i,2}^{2} + (1-p_{j})\left(\frac{\mu_{1}}{\mu_{2}}\xi_{pi,2} - \frac{\mu_{1}}{\mu_{2}}\gamma_{i,2}\right)^{2}\right]\right) \\ - \left(p_{i}\left[\left(\frac{\mu_{1} + \mu_{2}}{\mu_{2}}\right)^{2}\lambda_{i,2}^{2} + (1-p_{j})\left(\frac{\mu_{1} + \mu_{2}}{\mu_{2}}\xi_{pi,2} - \frac{\mu_{1} + \mu_{2}}{\mu_{2}}\gamma_{i,2}\right)^{2}\right]\right) \\ + \left(p_{i}\left[\left(\frac{\mu_{1} + \mu_{2}}{\mu_{1}}\right)^{2}\lambda_{i,1}^{2} + (1-p_{j})\left(\frac{\mu_{1} + \mu_{2}}{\mu_{1}}\xi_{pi,1} - \frac{\mu_{1} + \mu_{2}}{\mu_{1}}\gamma_{i,1}\right)^{2}\right]\right)\right] \end{cases}$$

[A6]

And the statistical test:

$$\begin{split} T_{GLi} &= \frac{\hat{G}L_{I} - \hat{G}L_{I}}{\left[ \left( \begin{array}{c} 2 \left( p_{i} \left[ \lambda_{i,2}^{2} + \left( 1 - p_{j} \right) \left( \xi_{pi,2} - \gamma_{i,2} \right)^{2} \right] \right) / N_{2} + 2 \left( p_{i} \left[ \left( \frac{\mu_{1}}{\mu_{2}} \right)^{2} \lambda_{i,2}^{2} + \left( 1 - p_{j} \right) \left( \frac{\mu_{1}}{\mu_{2}} \xi_{pi,2} - \frac{\mu_{1}}{\mu_{2}} \gamma_{i,2} \right)^{2} \right] \right) / N_{2}} \right] + \left( \frac{p_{i} \left[ \left( \frac{\mu_{1} + \mu_{2}}{\mu_{2}} \right)^{2} \lambda_{i,2}^{2} + \left( 1 - p_{j} \right) \left( \frac{\mu_{1} + \mu_{2}}{\mu_{2}} \xi_{pi,2} - \frac{\mu_{1} + \mu_{2}}{\mu_{2}} \gamma_{i,2} \right)^{2} \right] \right) / N_{2}} \right] \\ &+ \left( p_{i} \left[ \left( \frac{\mu_{1} + \mu_{2}}{\mu_{1}} \right)^{2} \lambda_{i,1}^{2} + \left( 1 - p_{j} \right) \left( \frac{\mu_{1} + \mu_{2}}{\mu_{1}} \xi_{pi,1} - \frac{\mu_{1} + \mu_{2}}{\mu_{1}} \gamma_{i,1} \right)^{2} \right] \right) / N_{1}} \right] \right] \\ para i = 1, 2, \dots, K. \qquad [A7] \end{split}$$

In this expression, all the variables re known or can be calculated.

## ANNEX

Decile	$\hat{G}L_1$	$\hat{G}L_2$	$T_{GLi}$	Sig.	$\hat{G}L_{I}$	$T_{GLi}$	Sig.
1	372,02	548,45	-21,69	***	541,04	-19,04	***
2	1045,46	1355,04	-25,50	***	1336,16	-22,16	***
3	1865,43	2315,71	-27,91	***	2282,92	-23,97	***
4	2820,18	3404,27	-28,31	***	3355,21	-23,81	***
5	3919,35	4624,49	-27,63	***	4556,65	-23,09	***
6	5169,11	5985,61	-26,58	***	5898,39	-21,87	***
7	6591,56	7510,77	-25,00	***	7400,22	-20,33	***
8	8232,49	9247,72	-23,17	***	9109,92	-18,57	***
9	10218,05	11308,83	-20,46	***	11139,39	-16,05	***
10	14212,63	14438,36	-1,79		14212,63	0,00	

Table A.2 France: 1993-2006

Table A.8 France: 2000-2006

Decile	$\hat{G}L_1$	$\hat{G}L_2$	$T_{GLi}$	Sig.	$\hat{G}L_I$	$T_{GLi}$	Sig.
1	522,97	548,45	-3,17	**	554,10	-3,61	***
2	1308,89	1355,04	-3,56	***	1369,83	-4,21	***
3	2260,32	2315,71	-3,14	**	2340,85	-4,07	***
4	3353,11	3404,27	-2,25		3440,46	-3,40	***
5	4594,20	4624,49	-1,06		4674,87	-2,48	
6	5985,89	5985,61	0,01		6049,76	-1,63	
7	7550,41	7510,77	0,97		7593,16	-0,93	
8	9325,17	9247,72	1,59		9349,50	-0,44	
9	11447,91	11308,83	2,34		11434,02	0,21	
10	14597,57	14438,36	1,80		14597,57	0,00	

Table A.7 France: 1993-2000

Decile	$\hat{G}L_1$	$\hat{G}L_2$	$T_{GLi}$	Sig.	$\hat{G}L_I$	$T_{GLi}$	Sig.
1	372,02	522,97	-17,17	***	511,09	-13,36	***
2	1045,46	1308,89	-18,71	***	1277,30	-14,69	***
3	1865,43	2260,32	-20,69	***	2205,33	-16,40	***
4	2820,18	3353,11	-21,52	***	3271,51	-17,25	***
5	3919,35	4594,20	-21,77	***	4480,15	-17,53	***
6	5169,11	5985,89	-21,79	***	5839,07	-17,66	***
7	6591,56	7550,41	-21,60	***	7362,30	-17,44	***
8	8232,49	9325,17	-20,61	***	9090,65	-16,53	***
9	10218,05	11447,91	-19,03	***	11158,29	-15,07	***
10	14212,63	14597,57	-2,87	**	14212,63	0,00	

Decile	$\hat{G}L_1$	$\hat{G}L_2$	$T_{GLi}$	Sig.	$\hat{G}L_I$	$T_{GLi}$	Sig.
1	169,69	256,17	-16,63	***	236,89	-10,85	***
2	555,66	716,75	-17,41	***	658,76	-10,01	***
3	1053,13	1295,76	-19,12	***	1188,94	-9,89	***
4	1646,63	1987,44	-20,21	***	1822,08	-9,83	***
5	2344,06	2799,61	-21,52	***	2565,01	-10,05	***
6	3155,91	3727,09	-22,32	***	3413,14	-9,85	***
7	4101,95	4770,11	-21,94	***	4365,83	-8,63	***
8	5208,52	5959,27	-21,29	***	5449,78	-6,91	***
9	6521,78	7343,68	-19,94	***	6710,18	-4,67	***
10	8610,04	9434,52	-13,83	***	8610,04	0,00	

Table A.9 Italy: 1993-2000

Table A.10 Italy: 2000-2006

Decile	$\hat{G}L_1$	$\hat{G}L_2$	$T_{GLi}$	Sig.	$\hat{G}L_I$	$T_{GLi}$	Sig.
1	256,17	316,97	-11,68	***	237,00	3,32	***
2	716,75	897,15	-20,94	***	672,46	4,31	***
3	1295,76	1623,59	-27,61	***	1216,84	5,58	***
4	1987,44	2489,92	-31,41	***	1865,98	6,33	***
5	2799,61	3505,80	-35,15	***	2627,95	7,13	***
6	3727,09	4668,91	-38,80	***	3499,91	7,87	***
7	4770,11	6003,82	-43,16	***	4503,68	7,94	***
8	5959,27	7552,96	-47,99	***	5673,34	7,45	***
9	7343,68	9424,02	-53,12	***	7093,55	5,64	***
10	9434,52	12473,11	-52,08	***	9434,52	0,00	

#### Table A.3 Italy: 1993-2006

Decile	$\hat{G}L_1$	$\hat{G}L_2$	$T_{GLi}$	Sig.	$\hat{G}L_I$	$T_{GLi}$	Sig.
1	169,69	316,97	-29,58	***	229,77	-10,95	***
2	555,66	897,15	-42,86	***	633,50	-8,34	***
3	1053,13	1623,59	-52,73	***	1135,87	-6,59	***
4	1646,63	2489,92	-59,73	***	1734,74	-5,44	***
5	2344,06	3505,80	-65,94	***	2437,02	-4,60	***
6	3155,91	4668,91	-70,75	***	3237,82	-3,35	***
7	4101,95	6003,82	-73,38	***	4153,86	-1,74	
8	5208,52	7552,96	-77,13	***	5215,24	-0,19	
9	6521,78	9424,02	-80,21	***	6501,20	0,51	
10	8610,04	12473,11	-70,70	***	8610,04	0,00	

Decile	$\hat{G}L_1$	$\hat{G}L_2$	$T_{GLi}$	Sig.	$\hat{G}L_I$	$T_{GLi}$	Sig
1	181,29	223,85	-9,55	***	204,32	-5,01	***
2	517,02	607,86	-12,29	***	553,56	-4,89	***
3	941,04	1090,93	-14,43	***	993,18	-5,03	***
4	1443,75	1660,52	-16,20	***	1511,24	-5,11	***
5	2027,44	2317,65	-16,88	***	2108,59	-4,85	***
6	2702,35	3080,01	-17,96	***	2801,27	-4,89	***
7	3488,95	3956,15	-17,87	***	3597,58	-4,38	***
8	4437,11	4994,75	-17,62	***	4539,66	-3,44	***
9	5633,65	6261,29	-15,81	***	5688,61	-1,49	
10	7579,51	8347,71	-12,49	***	7579,51	0,00	

Table A.5 Spain: 1993-2000

Table A.6 Spain: 2000-2006

Decile	$\hat{G}L_1$	$\hat{G}L_2$	$T_{GLi}$	Sig.	$\hat{G}L_I$	$T_{GLi}$	Sig.
1	223,85	226,51	-0,60		216,46	1,50	
2	607,86	637,98	-4,10	***	610,19	-0,28	
3	1090,93	1152,44	-5,99	***	1102,24	-0,97	
4	1660,52	1764,82	-7,79	***	1688,09	-1,84	
5	2317,65	2483,06	-9,63	***	2375,53	-2,99	**
6	3080,01	3312,91	-11,10	***	3170,31	-3,83	***
7	3956,15	4266,83	-11,97	***	4083,09	-4,32	***
8	4994,75	5379,23	-12,52	***	5147,87	-4,44	***
9	6261,29	6720,78	-12,12	***	6430,36	-3,94	***
10	8347,71	8728,52	-6,60	***	8347,71	0,00	

Table A.1Spain. Period 1993-2006

Decil	$\hat{G}L_1$	$\hat{G}L_2$	$T_{GLi}$	Sig.	$\hat{G}L_I$	$T_{GLi}$	Sig.
1	181,29	226,51	-11,75	***	197,86	-4,18	***
2	517,02	637,98	-19,69	***	556,66	-6,25	***
3	941,04	1152,44	-24,80	***	1005,22	-7,25	***
4	1443,75	1764,82	-28,73	***	1539,18	-8,37	***
5	2027,44	2483,06	-32,06	***	2165,81	-9,51	***
6	2702,35	3312,91	-35,11	***	2889,87	-10,51	***
7	3488,95	4266,83	-36,47	***	3721,40	-10,55	***
8	4437,11	5379,23	-36,08	***	4688,34	-9,09	***
9	5633,65	6720,78	-33,86	***	5851,40	-6,33	***
10	7579,51	8728,52	-25,45	***	7579,51	0,00	

Decile	$\hat{G}L_1$	$\hat{G}L_2$	$T_{GLi}$	Sig.	$\hat{G}L_I$	$T_{GLi}$	Sig.
1	187,85	333,39	-21,10	***	264,01	-25,52	***
2	568,86	875,35	-31,08	***	680,84	-21,98	***
3	1066,60	1538,85	-41,86	***	1186,39	-17,12	***
4	1657,95	2321,43	-51,65	***	1781,17	-13,36	***
5	2346,55	3218,60	-57,18	***	2462,73	-9,81	***
6	3140,00	4241,97	-43,15	***	3237,97	-5,14	***
7	4056,93	5410,08	-44,03	***	4121,60	-2,88	**
8	5123,81	6768,90	-44,10	***	5150,21	-0,99	
9	6431,44	8405,38	-44,95	***	6383,24	1,57	
10	8381,06	11025,18	-33,14	***	8381,06	0,00	

Table A.11 UK: 1993-2000

Table A.12 UK: 2000-2006

Decile	$\hat{G}L_1$	$\hat{G}L_2$	$T_{GLi}$	Sig.	$\hat{G}L_I$	$T_{GLi}$	Sig.
1	333,39	553,98	-23,15	***	296,86	3,18	**
2	875,35	1473,18	-41,68	***	794,57	5,08	***
3	1538,85	2616,76	-57,44	***	1417,77	6,89	***
4	2321,43	3964,10	-69,90	***	2152,71	8,75	***
5	3218,60	5534,26	-78,03	***	3013,63	9,11	***
6	4241,97	7343,69	-77,00	***	4010,56	5,69	***
7	5410,08	9412,87	-82,42	***	5151,55	5,29	***
8	6768,90	11828,96	-85,79	***	6484,45	4,80	***
9	8405,38	14796,43	-88,94	***	8137,39	3,81	***
10	11025,18	19859,12	-64,21	***	11025,18	0,00	

Table A.4 UK: 1993-2006

Decile	$\hat{G}L_1$	$\hat{G}L_2$	$T_{GLi}$	Sig.	$\hat{G}L_I$	$T_{GLi}$	Sig.
1	187,85	553,98	-52,2	***	265,27	-17,76	***
2	568,86	1473,18	-79,9	***	657,94	-12,02	***
3	1066,60	2616,76	-95,6	***	1130,21	-6,17	***
4	1657,95	3964,10	-108,6	***	1682,99	-1,87	
5	2346,55	5534,26	-116,7	***	2328,20	1,09	
6	3140,00	7343,69	-125,7	***	3070,97	3,32	***
7	4056,93	9412,87	-132,9	***	3914,64	5,67	***
8	5123,81	11828,96	-137,3	***	4902,13	7,30	***
9	6431,44	14796,43	-140,0	***	6116,26	9,05	***
10	8381,06	19859,12	-99,4	***	8381,06	0,00	